

Computational Aerodynamics Questions & Answers

Question by Student 201238707

when we found velocity vector u_1^{n+1} & v_1^{n+1} . we extrapolated $u_1^{n+\frac{1}{2}}$ & $v_1^{n+\frac{1}{2}}$. And we put $\theta_1^{n+\frac{1}{2}} = \theta_1^{n+1}$ then used

$$\theta_1^{n+1} = \text{atan}\left(\frac{v_1^{n+1}}{u_1^{n+1}}\right) = \text{atan}\left(\frac{\alpha * v_1^{n+\frac{1}{2}}}{\alpha * v_1^{n+\frac{1}{2}}}\right)$$

but i wonder why those θ are same?

I don't understand. What other value would you give it?

Question by Student 201227147

Professor, in the section 2 of the table (Euler Equation in Generalized Coordinates), it says that $Q \equiv \Omega U$. But I guess it should be $Q \equiv \Omega \Gamma U$.

True, but $\Gamma = 1$, so it doesn't matter in this case. 1 point bonus.

Question by Student 201327132

$$\begin{aligned}
 \frac{\partial \Omega}{\partial \tau} &= \frac{\partial}{\partial \tau} (x_5 y_7 - y_5 x_7) \\
 &= \left(\frac{\partial}{\partial \xi} \frac{\partial x}{\partial \tau} \right) \frac{\partial y}{\partial \eta} + \left(\frac{\partial}{\partial \eta} \frac{\partial y}{\partial \tau} \right) \frac{\partial x}{\partial \xi} \\
 &\quad - \left(\frac{\partial}{\partial \xi} \frac{\partial y}{\partial \tau} \right) \frac{\partial x}{\partial \eta} - \left(\frac{\partial}{\partial \eta} \frac{\partial x}{\partial \tau} \right) \frac{\partial y}{\partial \xi} \\
 &= \left[\frac{\partial}{\partial \xi} \left(\frac{\partial x}{\partial \eta} \frac{\partial \eta}{\partial \tau} \right) \right] \frac{\partial y}{\partial \eta} + \left[\frac{\partial}{\partial \eta} \left(\frac{\partial y}{\partial \xi} \frac{\partial \xi}{\partial \tau} \right) \right] \frac{\partial x}{\partial \xi} \\
 &\quad - \left[\frac{\partial}{\partial \xi} \left(\frac{\partial y}{\partial \eta} \frac{\partial \eta}{\partial \tau} \right) \right] \frac{\partial x}{\partial \eta} - \left[\frac{\partial}{\partial \eta} \left(\frac{\partial x}{\partial \xi} \frac{\partial \xi}{\partial \tau} \right) \right] \frac{\partial y}{\partial \xi} \\
 \frac{\partial \Omega}{\partial \tau} &= \cancel{\frac{\partial^2 x}{\partial \xi \partial \eta} \frac{\partial y}{\partial \tau}} + \cancel{\frac{\partial^2 y}{\partial \xi \partial \eta} \frac{\partial x}{\partial \tau}} + \cancel{\frac{\partial^2 y}{\partial \eta \partial \xi} \frac{\partial x}{\partial \tau}} + \cancel{\frac{\partial^2 x}{\partial \eta \partial \xi} \frac{\partial y}{\partial \tau}} \\
 &\quad - \cancel{\frac{\partial^2 y}{\partial \xi \partial \eta} \frac{\partial x}{\partial \tau}} - \cancel{\frac{\partial^2 x}{\partial \xi \partial \eta} \frac{\partial y}{\partial \tau}} - \cancel{\frac{\partial^2 x}{\partial \eta \partial \xi} \frac{\partial y}{\partial \tau}} - \cancel{\frac{\partial^2 y}{\partial \eta \partial \xi} \frac{\partial x}{\partial \tau}} = 0
 \end{aligned}$$

$\boxed{\frac{\partial \Omega}{\partial \tau} = 0}$

Professor, This is answer of thursday question. It is not relate that mesh doesn't change in time.

This is great! 2.0 points bonus. I would have given you 3 points bonus if you would have typeset it using L^AT_EX.

Question by Student 201327132

Professor, Assignment 2 deadline is described Tuesday 29th March. So That confused me.

Its due on Thursday. I fixed the mistake.

Question by Student 201327133

Professor, I have a question about τ . I understood that η and ξ mean each line number of horizontal and vertical grid. But i don't know what is physical meaning of τ . If i know that, it much easier to understand the class.

τ is the same as t because we set Γ to 1. 1 point bonus.

Question by Student 201327103

Professor, I think the problem is i and x are not in same direction. In previous example, i axis and x axis are in same direction. So that computer can decide x component first with setted space and than decide y component form equation

$$y = \sin(15x/L)H/20$$

Here the space doesn't change with y But in this problem space change with x and y . So, computer may not find proper point of nodes which have setted space through $x^2 + y^2 = r^2$. Because I don't know the computer codes in detail, I can't approach to the solution.

You're on the right track. It has something to do with the fact that it's difficult to find a root for y on a circle at $x = \pm r_i$. Because the method used to solve the equation within the Equation() command is a Newton-Raphson non-linear root solver, it may fail close to $x = \pm r_i$ depending on the initial guess or the size of the first Δx given to the solver. Say for example that x is at $-r_i$ and Δx is set to -10^{-10} m, then this will result in a negative value for y^2 in the Newton-Raphson procedure, and the Equation command will fail. I'll explain this better through an example next class. 2 points bonus.